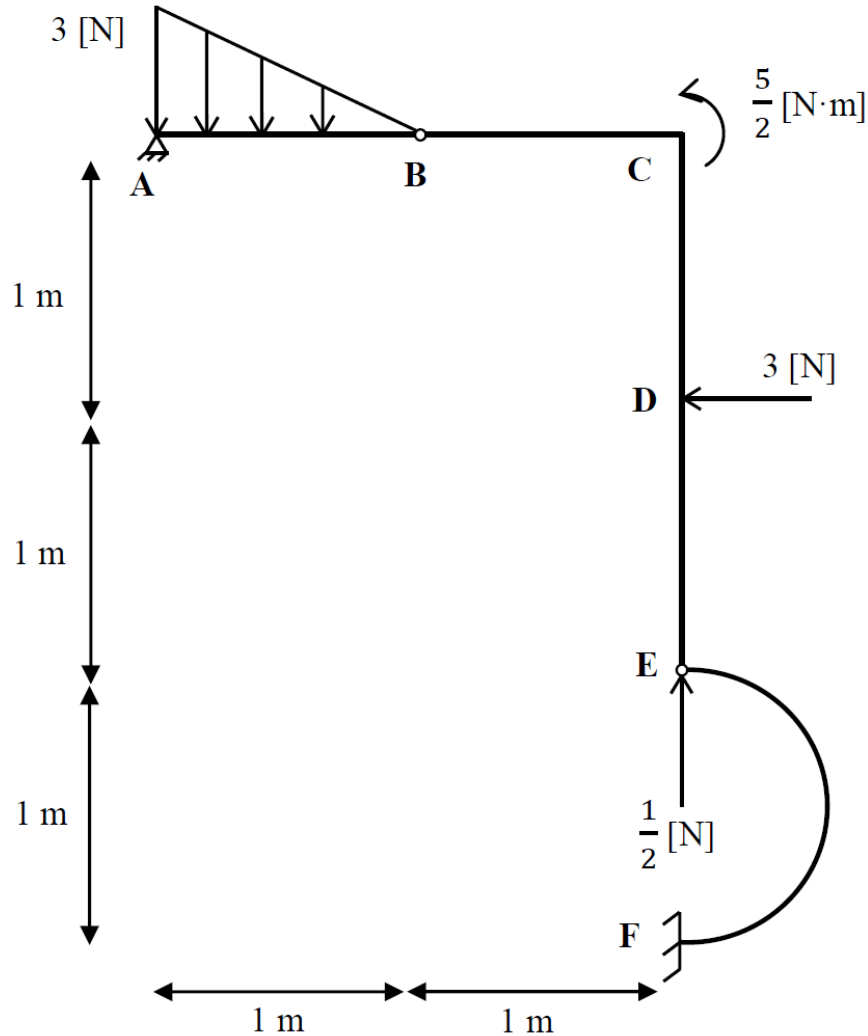


Determine the global degree of static indeterminacy (DSI) . If possible, calculate the reaction forces at the supports of the next structure. Determine its force laws and bending moments laws. Draw its corresponding diagrams.



### 1) Degree of static indeterminacy

$$\text{EDSI} = 5 - 3 = 2$$

$$\text{IDOF} = 3(4 - 1) = 9$$

$$\text{IL} = 2[2(2 - 1)] + 3(2 - 1) = 7$$

$$\text{IDSI} = 7 - 9 = -2$$

$$\text{DSI} = \text{EDSI} + \text{IDSI} = 2 - 2 = 0$$

Therefore, the structure is completely linked and the reactions are statically determined. Now, we are going to use the equations of equilibrium to solve it.

## 2) Reaction forces

$$\sum M_B = 0 \rightarrow V_A - \frac{1}{2} \cdot 3 \cdot 1 \cdot \frac{2}{3} = 0 \rightarrow V_A = 1 \text{ N}$$

$$\sum F_y = 0 \rightarrow V_A + V_F + \frac{1}{2} = \frac{3}{2} \rightarrow V_F = 0 \text{ N}$$

$$\sum M_E = 0 \rightarrow 2 \cdot V_A + 2 \cdot H_A - \frac{1}{2} \cdot 3 \cdot 1 \cdot \frac{5}{3} - \frac{5}{2} - 3 \cdot 1 = 0 \rightarrow H_A = 3 \text{ N}$$

$$\sum F_x = 0 \rightarrow H_F = 0 \text{ N}$$

$$\sum M_E = 0 \rightarrow M_F = 0 \text{ N} \rightarrow \text{Then it is not necessary to analyze the arch!!}$$

## 3) Force laws diagrams

### Stretch AB

$$N_{AB} = -3 \text{ N}$$

$$q(x) = q_0 \left(1 - \frac{x}{L}\right) = 3(1 - x)$$

$$V_T(x) = \int_0^x q_0 \left(1 - \frac{\xi}{L}\right) d\xi = \left[ q_0 \left(\xi - \frac{\xi^2}{2L}\right) \right]_0^x = 3 \left(x - \frac{x^2}{2}\right)$$

$$V_{AB} = 1 - 3 \left(x - \frac{x^2}{2}\right) = \frac{3x^2}{2} - 3x + 1 \text{ N}$$

$$M_T(x) = \int_0^x q_0 \left(\xi - \frac{\xi^2}{2L}\right) d\xi = \left[ q_0 \left(\frac{\xi^2}{2} - \frac{\xi^3}{6L}\right) \right]_0^x = 3 \left(\frac{x^2}{2} - \frac{x^3}{6}\right)$$

$$M_{AB} = x - 3 \left(\frac{x^2}{2} - \frac{x^3}{6}\right) = \frac{x^3}{2} - \frac{3x^2}{2} + x \text{ N.m}$$

$$M_{\max} \rightarrow \frac{dM(x)}{dx} = V(x) = 0 \rightarrow x = 0,47 \text{ m} \rightarrow M_{\max} = 0,192 \text{ N.m}$$

### Stretch BC

$$N_{BC} = -3 \text{ N}$$

$$V_{BC} = -\frac{3}{2} + 1 = -\frac{1}{2} \text{ N}$$

$$M_{BC} = -x - \frac{3}{2} \left(x - \frac{1}{3}\right) = -\frac{x}{2} + \frac{1}{2} \text{ N.m}$$

Stretch CD

$$N_{CD} = -0,5 \text{ N}$$

$$V_{CD} = 3 \text{ N}$$

$$V_{CD} = 3y - 3 \text{ N.m}$$

Stretch ED

$$N_{ED} = -0,5 \text{ N}$$

$$V_{ED} = 0 \text{ N}; M_{ED} = 0 \text{ N.m}$$

4) Force laws diagrams

